

4-4**Reteaching** (continued)**Factoring Quadratic Expressions**

- $a^2 + 2ab + b^2 = (a + b)^2$ Factoring perfect square trinomials
- $a^2 - 2ab + b^2 = (a - b)^2$
- $a^2 - b^2 = (a + b)(a - b)$ Factoring a difference of two squares

Problem

What is $25x^2 - 20x + 4$ in factored form?

There are three terms. Therefore, the expression may be a perfect square trinomial.

$$a^2 = 25x^2 \text{ and } b^2 = 4 \quad \text{Find } a^2 \text{ and } b^2.$$

$$a = 5x \text{ and } b = 2 \quad \text{Take square roots to find } a \text{ and } b.$$

Check that the choice of a and b gives the correct middle term.

$$2ab = 2 \cdot 5x \cdot 2 = 20x$$

Write the factored form.

$$a^2 - 2ab + b^2 = (a - b)^2$$

$$25x^2 - 20x + 4 = (5x - 2)^2$$

Check $(5x - 2)^2$ You can check your answer by multiplying the factors together.
 $(5x - 2)(5x - 2)$ Rewrite the square in expanded form.
 $25x^2 - 10x - 10x + 4$ Distribute.
 $25x^2 - 20x + 4$ Simplify.

Exercises

Factor each expression.

23. $x^2 - 12x + 36$

24. $x^2 + 30x + 225$

25. $9x^2 - 12x + 4$

26. $x^2 - 64$

27. $9x^2 - 42x + 49$

28. $25x^2 - 1$

29. $27x^2 - 12$

30. $49x^2 + 42x + 9$

31. $16x^2 - 32x + 16$

32. $9x^2 - 16$

33. $8x^2 - 18$

34. $81x^2 + 126x + 49$

35. $125x^2 - 100x + 20$

36. $-x^2 + 196$

37. $-16x^2 - 24x - 9$